Using aluminum nitride photonic-chip waveguides, we generate optical-frequency-comb supercontinuum spanning from 500 to 4000 nm with a 0.8-nJ seed pulse, and we show that the spectrum can be tailored by changing the waveguide geometry. Since aluminum nitride exhibits both quadratic and cubic nonlinearities, the spectra feature simultaneous contributions from numerous nonlinear mechanisms: supercontinuum generation, difference-frequency generation, second-harmonic generation, and third-harmonic generation. As one application of integrating multiple nonlinear processes, we measure and stabilize the carrier-envelope-offset frequency of a laser comb by direct photodetection of the output light. Additionally, we generate approximately 0.3 mW of broadband light in the 3000- and 4000-nm spectral region, which is potentially useful for molecular spectroscopy. The combination of broadband light generation from the visible through the midinfrared, combined with simplified self-referencing, provides a path towards robust comb systems for spectroscopy and metrology in the field.

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I. INTRODUCTION

Optical frequency combs are laser-based light sources that enable a wide variety of precision measurements, including the comparison of state-of-the-art atomic clocks [1], the quantitative measurement of pollution over several-kilometer paths above cities [2,3], and even the search for distant Earth-like planets [4,5]. Laser frequency combs are typically generated with relatively narrow (about 10%) relative spectral bandwidth [6]. However, a broad bandwidth is a requirement for many applications, such as spectroscopy, where it is desirable to probe several atomic or molecular transitions simultaneously, and optical frequency metrology, where stable lasers at different wavelengths must be compared. Consequently, narrowband frequency combs are usually spectrally broadened to at least one octave via supercontinuum generation (SCG) in materials with cubic nonlinearity (χ(3)), such as highly nonlinear fiber (HNLF) or photonic-crystal fiber [7].

Moreover, octave-spanning bandwidth allows the carrier-envelope-offset frequency (f_{CEO}) of the frequency comb to be measured (and subsequently stabilized) using “f-2f” self-referencing [8–10]. In the f-2f scheme, the low-frequency portion of the spectrum undergoes second-harmonic generation (SHG) in a material with quadratic nonlinearity (χ(2)), such as LiNbO₃, and interferes with the high-frequency portion of the spectrum, producing a signal that oscillates at f_{CEO}. Because of the modest effective nonlinearity of silica HNLF, SCG using traditional silica fiber requires high peak powers (typically 10 kW or more), which increases the electrical power requirements of the laser and limits the achievable repetition rates. Indeed, the adoption of compact frequency-comb sources at gigahertz repetition rates, such as electro-optic combs [11,12] and microresonator combs [6,13,14], is currently hindered by the difficulty of generating octave-spanning spectra using low-peak-power pulses. In addition, many potential applications for frequency combs require supercontinuum light at wavelengths that are difficult to achieve with SCG in silica fiber. For example, light in the midinfrared (3- to 8-μm) region is advantageous for molecular spectroscopy [15–19], but it is absorbed by silica fiber.

Fortunately, on-chip photonic waveguides with wavelength-scale dimensions offer high confinement of light, which provides a substantial increase in the effective nonlinearity,
\[
\gamma = \frac{2\pi n_2}{\lambda A_{\text{eff}}} \quad (1)
\]

where \(\lambda\) is the wavelength, \(A_{\text{eff}}\) is the effective area of the mode, and \(n_2\) is the material-dependent nonlinear index, which is directly proportional to \(\chi^{(3)}\) [7]. In addition, materials with a higher \(\chi^{(3)}\)—such as silicon nitride [20–27], silicon [28–30], aluminum gallium arsenide [31], and chalcogenide materials [32,33]—further increase \(\gamma\) and allow much lower peak power (<1 kW) to be used for the SCG process. High-confinement waveguides provide the additional advantage of increased control over the group-velocity dispersion (GVD), and therefore the spectral output of the SCG process.

Currently, supercontinuum generation in materials with both strong \(\chi^{(2)}\) and \(\chi^{(3)}\) is opening alternative possibilities for broadband light sources. For example, experiments with periodically poled LiNbO\(_3\) (PPLN) have demonstrated supercontinuum generation via cascaded \(\chi^{(2)}\) processes, and the simultaneous generation of supercontinuum and harmonic light [34–36]. Recently, aluminum nitride (AlN) has emerged as a lithographically compatible material that exhibits both strong \(\chi^{(2)}\) and \(\chi^{(3)}\), in addition to a broad transparency window. Consequently, thin-film AlN is proving to be a versatile platform for nanophotonics, providing phase-matched SHG [37], frequency-comb generation [38], and ultraviolet light emission [39].

Here, we present our observations of SCG in lithographically fabricated, on-chip AlN waveguides and demonstrate that the platform provides exciting capabilities: (1) We observe SCG from 500 to 4000 nm, and we show that the spectrum can be tailored simply by changing the geometry of the waveguide. (2) We find that the material birefringence induces a crossing of the transverse-electric (TE) and transverse-magnetic (TM) modes, which enhances the spectral brightness in a narrow band, and that the spectral location of this band can be adjusted by changing the waveguide dimensions. (3) We observe bright SHG, which is phase matched via higher-order modes of the waveguide, as well as phase-mismatched difference-frequency generation (DFG), which produces broadband light in the 3500- to 5500-nm region. (4) We demonstrate that simultaneous SCG and SHG processes in an AlN waveguide allows \(f_{\text{CEO}}\) to be extracted directly from the photodetected output, with no need for an external SHG crystal, recombination optics, or delay stage. (5) We use this simple scheme to lock the \(f_{\text{CEO}}\) of a compact laser frequency comb, and we find that the stability of the locked \(f_{\text{CEO}}\) is comparable to a standard \(f/2f\) interferometer and is sufficient to support precision measurements.

II. EXPERIMENT

The fully SiO\(_2\)-clad AlN waveguides [38,40] have a thickness (height) of 800 nm, and a width that varies from 400 to 5100 nm. Near the entrance and exit facets of the chip, the waveguide width tapers to 150 nm in order to expand the mode and improve the coupling efficiency, which is estimated at -4 dB/facet, on average. We generate the supercontinuum by coupling into the waveguide approximately 80 mW of 1560-nm light from a compact, turnkey Er-fiber frequency comb [41], which produces pulses of approximately 80 fs at 100 MHz. The polarization of the light is controlled using achromatic quarter and half wave plates. The light is coupled into each waveguide using an aspheric lens (NA = 0.6) designed for 1550 nm. For output coupling, two different techniques are used, as shown in Fig. 1(b). In the case of \(f_{\text{CEO}}\) detection, the light is outcoupled using a visible-wavelength microscope objective (NA = 0.85) and then dispersed with a grating before illuminating a photodiode. Alternatively, when recording the spectrum, the light is collected by butt coupling an InF\(_3\) multimode fiber (NA = 0.26) at the exit facet of the chip. The waveguide output is then recorded using two optical spectrum analyzers (OSAs); a grating-based OSA is used to record the spectrum across the visible and near-infrared regions, while a Fourier-transform OSA extends the coverage to 5500 nm.

To model the supercontinuum generation, we perform numerical simulations using the nonlinear Schrödinger equation (NLSE), as implemented in the \texttt{PyNLO} package.

![SEM cross section](image)

**FIG. 1.** (a) Aluminum nitride (AlN) on-chip waveguides embedded in SiO\(_2\) tightly confine the light field, providing high nonlinearity. (b) To generate supercontinuum, 80-fs laser pulses (1560 nm, 800 pJ) are coupled into each waveguide. The broadband output is directed into an optical spectrum analyzer (OSA), or dispersed with a grating, where \(f_{\text{CEO}}\) is detected in the 780-nm region using a photodiode. The \(f_{\text{CEO}}\) signal is digitized using a field-programmable gate array (FPGA), which applies feedback to the laser pump diode.
The effective refractive indices and effective nonlinearities of the waveguides are calculated using the vector finite-difference mode solver of Fallahkhair et al. [46]. The NLSE includes $\chi^{(3)}$ effects and incorporates the full wavelength dependence of the effective index, but it does not take into account any $\chi^{(2)}$ effects, higher-order modes, or wavelength-dependent absorption. In the simulations, we use $n_2 = 2.3 \times 10^{-19} \text{m}^2/\text{W}$ for AlN [38], which is very similar to the value of $2.4 \times 10^{-19} \text{m}^2/\text{W}$ measured for silicon nitride [47].

III. RESULTS AND DISCUSSION

A. Supercontinuum from visible to midinfrared

When pumped in the lowest-order quasi-transverse-electric mode ($\text{TE}_{00}$), the AlN waveguides generate light (Fig. 2) from the blue portion of the visible region (approximately 500 nm) to the midinfrared (about 4000 nm). The broad peaks on both sides of the spectrum are the short- and long-wavelength dispersive waves [labeled SWDW and LWDW, respectively, in Figs. 2(b) and 2(c)], which are generated at locations determined by the GVD of the waveguide [7,48]. The broadband spectrum is a result of the flat GVD profile enabled by strong confinement of the light in these waveguides. The simulated spectra [Fig. 2(c)] reproduce the spectral location of the long- and short-wavelength dispersive waves. However, the NLSE simulations overestimate the light intensity in the dispersive waves compared to the experiment. One reason for this discrepancy is that the waveguide mode at 1560 nm does not have perfect overlap with modes at different wavelengths, and the effective nonlinearity is actually smaller than what is predicted by Eq. (1), which assumes perfect mode overlap. This effect is most pronounced at longer wavelengths, where the mode extends significantly outside of the waveguide and does not overlap well with the 1560-nm mode, which is mostly confined within the AlN waveguide.

When waveguide widths near 3500 nm are used, the supercontinuum shows high spectral intensity over a broad region from 1400 to 2800 nm, generally remaining within $-20 \text{ dB}$ of the transmitted pump intensity. This bright spectrum represents a promising source for molecular spectroscopy since OH-stretching transitions absorb in this region [49]. Indeed, sharp dips visible in the spectral intensity near 2700 nm are due to the absorption of water vapor in the OSA. Unfortunately, a sharp minimum in the spectrum near 2900 nm and decreased intensity at wavelengths longer than 2900 nm suggests that these midinfared wavelengths are not efficiently transmitted through the waveguides. This loss is likely due to OH absorption [50] in the SiO$_2$, since a significant fraction of the mode extends outside the AlN waveguide and into the SiO$_2$ cladding at these wavelengths. In the future, the use of a different cladding material could increase the output of midinfrared light. Nevertheless, the waveguides still produce usable, broadband light in the midinfrared region; for example, we estimate that the 2600-nm waveguide produces about 0.3 mW in the 3500- to 4000-nm spectral region, which is sufficient power for some applications [51,52]. Indeed, the midinfrared light is easily seen in Fig. 2(b), which presents spectra collected with just a few seconds of integration time for each spectrum.

B. Brightness enhancement via a mode crossing

In the 800- to 1200-nm region, a sharp peak is seen in the supercontinuum spectrum for waveguide widths $>1500$ nm [Figs. 2(b) and 3(c)], which is not explained.
by the NLSE. The location of the peak occurs at the wavelength where the refractive index of the lowest-order TE mode (TE\(_{00}\)) and a higher-order quasi-TM mode (TM\(_{10}\)) cross [Fig. 3(a)]. While such mode crossings are commonplace in Kerr-comb generation in microring resonators [53–55], they are not typically seen in supercontinuum generation in straight waveguides because the TE\(_{00}\) usually has the highest effective index at all wavelengths. In the case of AlN waveguides, the polarization-mode crossing occurs because AlN is a birefringent material, and the bulk index for the vertical (TM) polarization is higher than that for the horizontal (TE) polarization. At short wavelengths, where the waveguide geometry provides only a small modification to the refractive index, the TM modes tend to have the highest effective index. However, at longer wavelengths, geometric dispersion plays a larger role, lowering the effective index of the TM modes more than the TE modes and causing the polarization-mode crossing. Similarly, since modifications of the waveguide width tend to change the effective index of the TE modes more than the TM modes, the spectral location of the mode crossing also depends on the width of the waveguide [Fig. 3(b)].

A mode crossing causes a sharp feature in the GVD, which can allow for the phase matching of four-wave-mixing processes in spectral regions that would otherwise be phase mismatched [53,54]. Indeed, the crossing of the TE\(_{00}\) and TM\(_{10}\) modes enables a strong enhancement of the supercontinuum spectrum in a spectral region that is otherwise dim. In some cases, this mode crossing enables an enhancement of the spectral intensity by more than 20 dB. This enhancement enables an additional amount of control over the spectral output, providing a narrow, bright region that could, for example, be used to measure a heterodyne beat with a narrow-band atomic-clock laser. It is not clear why the crossing with the TM\(_{10}\) mode is clearly seen in the experiment, while the crossings with the higher-order TM modes are absent. Understanding which mechanism couples the modes—and how this coupling could be enhanced—would allow for further customization of the spectral output of this supercontinuum source.

C. Second-harmonic generation and difference-frequency generation

Since AlN has \(\chi^{(2)}\) nonlinearity, it is capable of three-wave-mixing processes, such as DFG, sum-frequency generation, and SHG. The thin AlN films used in this study are not single crystals but instead consist of many hexagonal columns, which have the crystal \(z\) axis oriented in the same (vertical) direction [40], but a random orientation for the other crystal axes. Consequently, while there is a strong \(\chi^{(2)}\) component in the vertical (TM) direction, the \(\chi^{(2)}\) in the horizontal (TE) direction is much weaker.

Indeed, we observe the strongest \(\chi^{(2)}\) effects with the laser in the TM\(_{00}\) mode. The brightest SHG results from situations where the phase velocity of the second harmonic in a higher-order mode is the same as the phase velocity of the fundamental wavelength in the lowest-order mode. This situation provides excellent phase matching, and we observe situations where the spectral intensity of the

\[\text{FIG. 3.} \quad \text{(a) As the wavelength increases, the refractive index of the fundamental TE mode (TE}_{00}\text{) crosses several TM modes. A waveguide width of 3500 nm is shown. (b) The spectral location of these polarization-mode crossings changes as a function of the waveguide width (shown) and thickness (not shown). (c) The crossing of the TE}_{00}\text{ and TM}_{10}\text{ modes (as calculated from only the bulk refractive index and the waveguide geometry) matches the location of the sharp peak in the experimental spectra.}\]

DANIEL D. HICKSTEIN et al.
PHYS. REV. APPLIED 8, 014025 (2017) 014025-4
second-harmonic light is on the same order of magnitude as that of the transmitted pump laser [Figs. 4(a) and 4(b)]. However, this phase-matching mechanism provides a phase-matching bandwidth of only a few nanometers. Additionally, we also see third-harmonic generation (THG), which is phase matched to higher-order modes of the waveguide.

Under TM pumping, the waveguides also produce broadband light in the 3500- to 5500-nm region via DFG [Figs. 4(a) and 4(b)]. This process corresponds to the difference frequency between the spectrally broadened pump (1400–1700 nm) and the long-wavelength dispersive wave (2000–2700 nm). As the waveguide width narrows and the dispersive wave moves to shorter wavelengths, the DFG is pushed to longer wavelengths, as determined by the conservation of (photon) energy. Indeed, for waveguide widths less than 1800 nm, the DFG moves to wavelengths longer than 5500 nm, which is outside the range of our OSA. Additionally, the DFG process is strongly phase mismatched, and the conversion efficiency is therefore low. However, in principle, it is possible to achieve phase matching by launching the pump laser into a higher-order mode of the waveguide.

![Graph showing supercontinuum generation](image)

**FIG. 4.** Supercontinuum generation from the lowest-order quasi-transverse-magnetic (TM) mode. (a) Experimental spectra from both the 1000- and 1700-nm-wide waveguides show simultaneous supercontinuum generation, second-harmonic generation (SHG), third-harmonic generation (THG), and difference-frequency generation (DFG). (b) Experimental spectra from all waveguide widths, showing that waveguide geometry affects the positions of the long-wavelength dispersive wave (LWDW), the DFG peaks, and the phase-matched SHG peaks.

### D. \( f_{\text{CEO}} \) detection and comb stabilization

Since AlN exhibits both \( \chi^{(2)} \) and a strong \( \chi^{(3)} \), \( f_{\text{CEO}} \) can be directly detected in the 780-nm region as a result of simultaneous SHG and SCG. Unlike a traditional \( f-2f \) measurement, no interferometer is needed to set the temporal overlap of the interfering beams, and no additional alignment is necessary. The only equipment required to detect \( f_{\text{CEO}} \) is a 780-nm bandpass filter and a photodetector. Since these AlN waveguides have the strongest \( \chi^{(2)} \) tensor component in the vertical direction, we observe the highest signal-to-noise ratio \( f_{\text{CEO}} \) signal when pumping in the TM\(_{00}\) mode. When TM pumping the 4800-nm-wide waveguide, we achieve a 37-dB SNR for the \( f_{\text{CEO}} \) peak [Fig. 5(a)]. Interestingly, the highest SNR \( f_{\text{CEO}} \) is obtained from phase-mismatched SHG in the larger width waveguides, despite the fact that much higher efficiency phase-matched SHG is seen for waveguide widths near 1000 nm.

We speculate that the poor mode overlap between the supercontinuum (in the TM\(_{00}\) mode) and the phase-matched second harmonic (in a higher-order TM mode) hinders detection of the \( f_{\text{CEO}} \). Indeed, a recent attempt to detect a \( f-3f \) signal in SiN waveguides found that mode overlap severely limits the achievable SNR [56]. In contrast, the phase-mismatched SHG that takes place in the fundamental mode compensates for low conversion efficiency with better overlap with the supercontinuum light. Furthermore, the highest SHG conversion likely takes place at the point of soliton fission, where the pulse is compressed and the peak intensity is the highest. This is the same point where most of the supercontinuum light is generated. Since the \( f \) and \( 2f \) signals are generated simultaneously and propagate in the same waveguide mode, temporal overlap is provided automatically. Nevertheless, in future implementations, on-chip mode converters [57] could be used to provide both phase-matched SHG and mode overlap, thereby providing a higher \( f_{\text{CEO}} \) signal.

With the \( f_{\text{CEO}} \) detected directly from the waveguide output [Fig. 1(b)], we can achieve glitch-free \( f_{\text{CEO}} \) locking of a compact frequency comb for several hours [Fig. 5(b)]. By recording the frequency of the \( f_{\text{CEO}} \) beat with an independent \( \Pi \)-type [58] frequency counter [Fig. 5(c)], we can verify that the \( f_{\text{CEO}} \) has been stabilized to a level comparable to what can be achieved with a traditional \( f-2f \) interferometer [41]. Unfortunately, thermal drifts in the input coupling prevent locking for more than a few hours without realignment. In the future, input and output coupling could be accomplished via fibers glued to the facets of the chip [59], which would effectively eliminate thermal drift in the coupling and enable long-term stabilization of the laser comb.
IV. CONCLUSION

In this paper, we demonstrate aluminum nitride, a lithographically compatible material with strong $\chi^{(2)}$ and $\chi^{(3)}$ nonlinearities, as a promising material for on-chip supercontinuum generation and frequency comb self-referencing. Broadband light from 500 to 4000 nm can be generated with only about 80 mW (0.8 nJ) of 1560-nm pump power in the waveguide. Aluminum nitride provides an unexpected level of control over the output spectrum. Specifically, the birefringence of the material enables a crossing of the TE and TM modes, which provides an enhancement in the spectral intensity by several orders of magnitude. In addition, we observe phase-mismatched difference-frequency generation across the 3500- to 5500-nm region, which, if phase matched, could provide a useful midinfrared light source. Moreover, fully phase matched second- and third-harmonic generation provide narrow-band light that is tunable across the visible region.

Simultaneous second-harmonic and supercontinuum generation processes allow for the simplified detection of $f_{\text{CEO}}$ using a single, monolithic waveguide and enable high-quality stabilization of a compact laser frequency comb. In conclusion, aluminum nitride waveguides provide both robust comb stabilization and access to broad spectra across the visible, near-infrared, and midinfrared regions. These capabilities are crucial ingredients for building inexpensive, portable frequency combs for field applications such as dual-comb spectroscopy, spectrograph calibration, and precision metrology.

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